

Suppose  $A$ ,  $B$ , and  $C$  are regular. Prove

$((\bar{A}) \circ B) \cup C^*$  is regular.

- $\bar{A}$  is regular (closure under  $\bar{\quad}$ )
- $C^*$  is regular (closure under  $*$ )
- $\bar{A} \circ B$  is regular (closure under  $\circ$ )
- $(\bar{A} \circ B) \cup C^*$  (closure under  $\cup$ )

Prove  $(00)^+ \cup (11)$  is regular.



$\therefore (00)^+$  and  $(11)$  are both regular languages.

$\therefore (00)^+ \cup 11$  is a regular language (closure under union)